

Anisotropic Hall effect in single-crystal heavy-fermion YbAgGe

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Temperature- and field-dependent Hall effect measurements are reported for YbAgGe, a heavy-fermion compound exhibiting a field-induced quantum phase transition, and for two other closely related members of the RAgGe series: a nonmagnetic analog, LuAgGe and a representative, “good local moment,” magnetic material, TmAgGe. Whereas the temperature-dependent Hall coefficient of YbAgGe shows behavior similar to what has been observed in a number of heavy-fermion compounds, the low temperature, field-dependent measurements reveal well-defined, sudden changes with applied field; in specific for $H \perp c$ a clear local maximum that sharpens as temperature is reduced below 2 K and that approaches a value of 45 kOe—a value that has been proposed as the $T=0$ quantum critical point. Similar behavior was observed for $H \parallel c$ where a clear minimum in the field-dependent Hall resistivity was observed at low temperatures. Although at our base temperatures it is difficult to distinguish between the field-dependent behavior predicted for (i) diffraction off a critical spin density wave or (ii) breakdown in the composite nature of the heavy electron, for both field directions there is a distinct temperature dependence of a feature that can clearly be associated with a field-induced quantum critical point at $T=0$ persisting up to at least 2 K.

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I. INTRODUCTION

Based on low temperature resistivity and heat capacity measurements in applied magnetic fields YbAgGe was recently classified as a new heavy-fermion material with long range, possibly small moment, magnetic order below 1 K^{1-4} that shows magnetic field-induced non-Fermi-liquid (NFL) behavior.² The critical field required to drive YbAgGe to the field-induced quantum critical point (QCP) is anisotropic ($H_c^{ab} \approx 45 \text{ kOe}$, $H_c^c \approx 80 \text{ kOe}$) and conveniently accessible by many experimental groups.² YbAgGe is one of the *rare earths* of intermetallics [apparently only second, after the extensively studied YbRh₂Si₂ (Refs. 5–8)] a *stoichiometric*, Yb-based, heavy fermion (HF) that shows magnetic field induced NFL behavior and as such is suitable to serve as a testing ground for experimental and theoretical constructions relevant for QCP physics. Among the surfeit of detailed descriptions developed for a material near the antiferromagnetic QCP we will refer to the outcomes⁹ of two more general, competing, pictures: in one viewpoint the QCP is a spin density wave (SDW) instability¹⁰ of the Fermi surface; within the second picture that originates in the description of heavy fermions as a Kondo lattice of local moments,^{11,12} heavy electrons are composite bound states formed between local moments and conduction electrons and the QCP is associated with the breakdown of this composite nature. It was suggested⁹ that Hall effect measurements can help distinguish which of these two mechanisms may be relevant for a particular material near a QCP. In the SDW scenario the Hall coefficient is expected to vary continuously through the quantum phase transition, whereas in the composite HF scenario the Hall coefficient is anticipated to change discontinuously at the QCP. Perhaps more importantly, in both scenarios a clear and sharp change in the field-dependent Hall effect (for the field-induced QCP) is

anticipated to occur at low temperatures, near the critical field value.

Although Hall effect measurements appear to be a very attractive method of gaining insight into the nature of the QCP, one has to keep in mind that an understanding of the different contributions to the measured Hall coefficient, in particular in magnetic or strongly correlated materials, is almost inevitably difficult and potentially evasive.^{13,14} Therefore measurements on samples well-characterized by other techniques^{1,2} as well as comparison with nonmagnetic as well as non-HF members of the same series can be beneficial. In this work we present temperature- and field-dependent Hall effect measurements on YbAgGe single crystals. The nonmagnetic member of the same RAgGe (R=rare earth) series, LuAgGe, and the magnetic, essentially nonhybridizing, TmAgGe were used for “commonsense” checks, or calipers, of the YbAgGe measurements.

II. EXPERIMENT

YbAgGe, LuAgGe, and TmAgGe single crystals in the form of clean, hexagonal-cross-section rods of several mm length and up to 1 mm^2 cross section were grown from high-temperature ternary solutions rich in Ag and Ge (see Ref. 1 for details of the samples' growth). Their structure and the absence of impurity phases were confirmed by powder x-ray diffraction. Temperature- and field-dependent Hall resistivity, $\rho_H(H, T)$, and auxiliary high-field magnetization measurements were performed down to 1.9 K in an applied magnetic field of up to 140 kOe in a Quantum Design PPMS-14 instrument. For YbAgGe Hall measurements were extended down to 0.4 K using the He-3 option of the PPMS-14. A four probe, ac technique ($f=16 \text{ Hz}$, $I=1-0.1 \text{ mA}$), was used for the Hall measurements. Samples were polished down to a

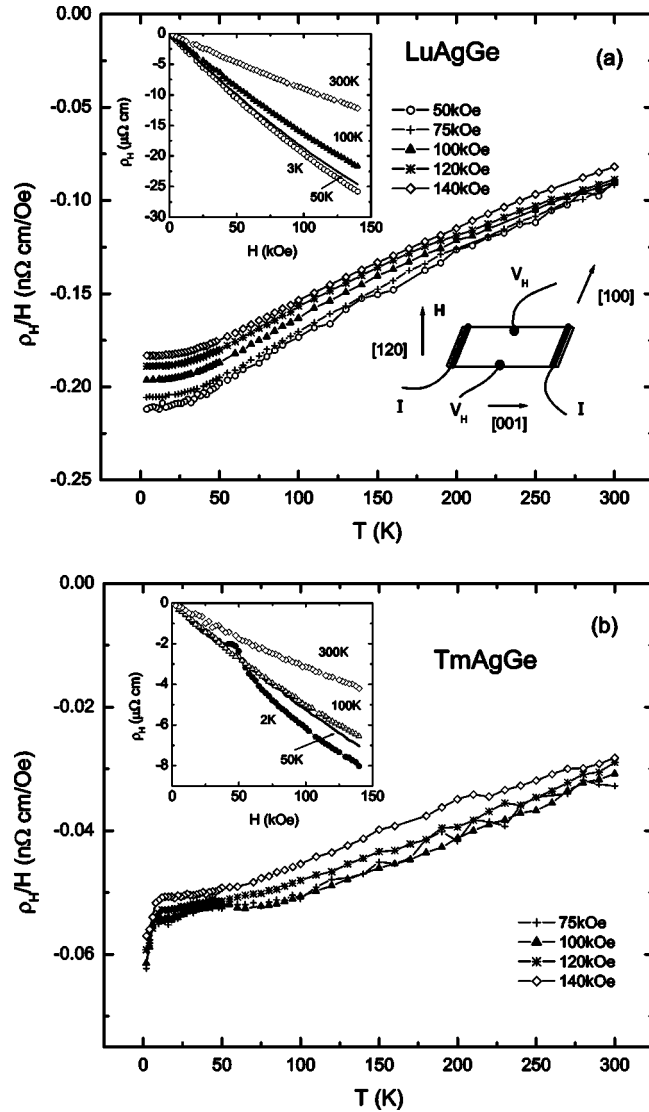


FIG. 1. (a) Temperature-dependent Hall coefficient, ρ_H/H , of LuAgGe measured in different applied fields ($H\parallel ab$). Upper inset: field-dependent Hall resistivity of LuAgGe measured at different temperatures. Lower inset: the sample, current, and applied field geometry used during the measurements. (b) Similar data for TmAgGe.

platelike shape with thicknesses of 0.3 to 0.4 mm. Pt leads were attached to the sample with Epotek H20E silver epoxy so that the current was flowing along the crystallographic c axis. For the $H\parallel ab$ case Hall resistivity (ρ_H) was measured in the hexagonal crystallographic plane (approximately along the [100] direction) with the magnetic field applied perpendicular to both the current and the Hall voltage directions (approximately along the [120] direction) (see the lower inset to Fig. 1). In the $H\parallel c$ case, current was flowing in the hexagonal plane, approximately in the [100] direction, and the Hall voltage was measured along the [120] direction. Due to rodlike morphology of the crystals, samples that were cut and polished for $H\parallel c$ measurements were smaller and the error bars in the absolute values (due to geometry and position of the contacts) are larger than for the $H\parallel ab$ data sets. To eliminate the effect of inevitable

(small) misalignment of the voltage contacts, the Hall measurements were taken for two opposite directions of the applied field, H and $-H$, and the odd component, $[\rho_H(H) - \rho_H(-H)]/2$, was taken as the Hall resistivity. To determine the Hall resistivity in the limit of low field, linear fits of the initial (linear) parts of the $\rho(H)$ data in both quadrants were used. He-4 Hall measurements for YbAgGe and LuAgGe were performed on two samples of each material, the results were the same within the error bars in sample dimensions and contact position measurements. During the measurements particular care was taken to avoid rotation and/or misplacement of the TmAgGe sample due to its magnetic anisotropy.

III. RESULTS AND DISCUSSION

A. LuAgGe and TmAgGe

The field-dependent Hall resistivity for LuAgGe for $H\parallel ab$ is shown in the upper inset to Fig. 1(a) for several temperatures. ρ_H is only slightly nonlinear in field over the whole temperature range. This minor nonlinearity causes some difference in the ρ_H/H vs T data obtained in different applied fields [Fig. 1(a)]. The Hall coefficient, $R_H = \rho_H/H$, is measured to be negative. The overall temperature dependence is monotonic, slow, and featureless with approximately a factor of 2 increase in the absolute value of ρ_H/H from room temperature to low temperatures. This temperature dependency of the Hall coefficient of the nonmagnetic material possibly reflects some details of its electronic structure [for example, comparable factor of 2 changes in R_H were recently observed in LaTIn_5 , $T=\text{Rh, Ir, Co}$ (Ref. 15)]. Overall the temperature and field dependence of the Hall coefficient for TmAgGe [Fig. 1(b)] is similar to that of LuAgGe with two main differences: (i) the long-range order and metamagnetism of TmAgGe (Ref. 1) is reflected in Hall measurements as a low temperature decrease in $R_H(T)$ and as anomalies in $\rho_H(H)$ for $T=2$ K that are consistent with the fields of the metamagnetic transitions; and (ii) the absolute values of the $R(H)$ data for TmAgGe are a factor of 3 to 4 smaller than for LuAgGe.

B. YbAgGe, $H\parallel ab$

The temperature-dependent Hall coefficient and the dc susceptibility data for YbAgGe with the same orientation of the magnetic field with respect to the crystallographic axis are shown in Fig. 2. The susceptibility, M/H , is field independent above 50 K [i.e., $M(H)$ is linear below 140 kOe in this temperature range] and is similar to the data reported in Refs. 1 and 2. The Hall coefficient, R_H , is field independent above approximately 25 K. The temperature dependencies of the susceptibility and the Hall coefficient at high temperatures closely resemble each other. At low temperatures a field-dependent maximum in R_H (see inset to Fig. 2) is observed. Qualitatively the temperature dependence of the Hall coefficient is consistent with the picture presented in Refs. 16–19 (see also Refs. 13 and 20 for a comprehensive review). Within this picture the temperature dependence of the Hall coefficient in heavy fermion materials is a result of two

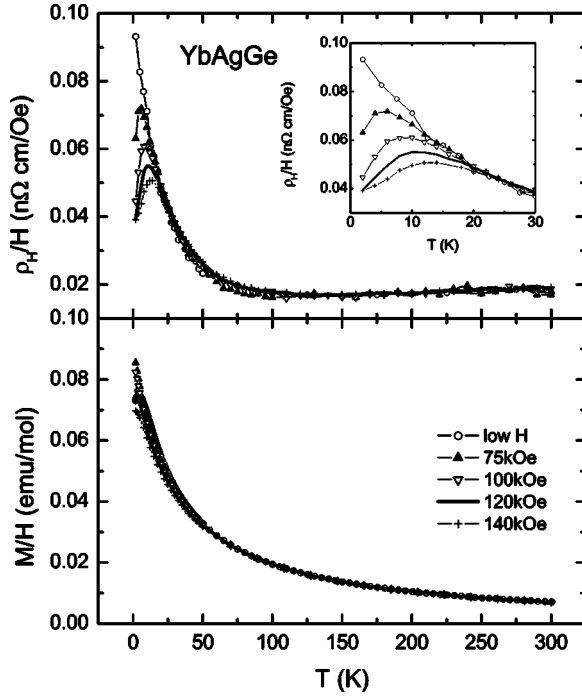


FIG. 2. Upper panel: temperature-dependent Hall coefficient, ρ_H/H , of YbAgGe measured in different applied fields ($H\parallel ab$). Inset: enlarged, low-temperature part of the data. Lower panel: dc susceptibility of YbAgGe (H along the $[120]$ direction). The “low H” label in the legend refers to the low-field Hall resistivity (see Sec. II) and susceptibility measured in $H=1$ kOe.

contributions: a residual Hall coefficient, $R_H^{res} = \rho_H^{res}/H$, and a Hall coefficient due to the intrinsic skew scattering, $R_H^s = \rho_H^s/H$. The residual Hall coefficient is ascribed to a combination of the ordinary Hall effect and residual skew scattering by defects and impurities and, to the first approximation, is considered to be temperature independent, although, realistically, both the ordinary Hall effect and the residual skew scattering may have weak temperature dependence. The temperature-dependent, intrinsic skew scattering contribution (R_H^s) at high-temperatures ($T \gg T_K$, where T_K is the Kondo temperature) increases as the temperature is lowered in a manner that is mainly due to the increasing magnetic susceptibility. At lower temperatures R_H^s passes through a crossover regime, then has a peak at a temperature on the order of the coherence temperature, T_{coh} , and finally, on further cooling rapidly decreases (in the coherent regime of skew scattering by fluctuations) to zero (i.e., R_H ultimately levels off to the $\sim R_H^{res}$ value at very low temperatures¹⁷⁻¹⁹). In the high temperature ($T \gg T_K$) limit we can (very roughly, within an order of magnitude) separate these two contributions to the observed temperature-dependent Hall coefficient using a phenomenological expression $R_H(T) = R_H^{res} + R_s \times \chi(T)$ (Ref. 21) with the temperature-dependent skew scattering contribution written as $R_H^s(T) = R_s \times \chi(T)$ where $\chi(T) = C/(T - \Theta)$, C is the Curie constant and Θ is the Weiss temperature. Using $\Theta_{ab} = -15.1$ K from Ref. 1 we can plot $R_H(T) \times (T - \Theta)$ vs $(T - \Theta)$ (Fig. 3) and from the linear part of the curve we can estimate $R_H^{res} \approx 0.02$ nΩ cm/Oe and $R_s \approx -0.17$ nΩ cm/Oe. It seems peculiar that our estimate of

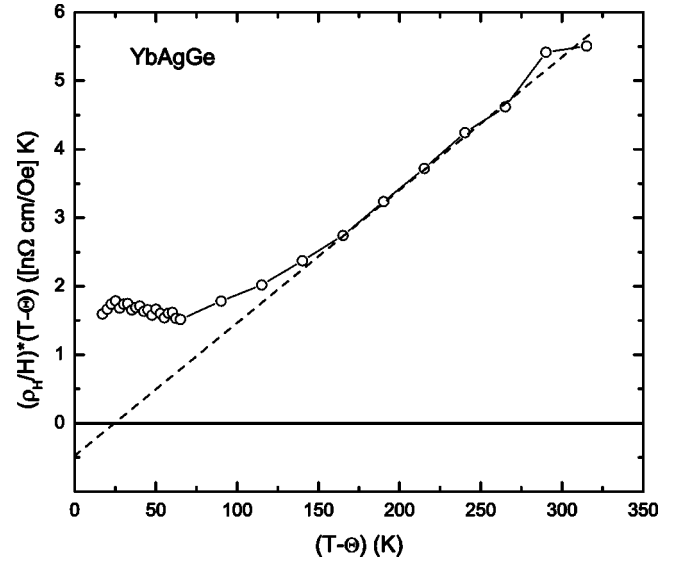


FIG. 3. Temperature-dependent low-field Hall coefficient ($H\parallel ab$) plotted as $(\rho_H/H) \times (T - \Theta)$ vs $(T - \Theta)$.

R_H^{res} for YbAgGe differs noticeably from the Hall coefficient measurements for LuAgGe and TmAgGe (see Fig. 1). Regarding this discrepancy it should be mentioned that besides possible experimental (mainly geometrical) errors these three materials may have different residual skew scattering and, additionally, as indicated by the preliminary results of band structure calculations,²² the density of states at the Fermi level can be considerably different for all three compounds under consideration. Although the magnetic susceptibility, $\chi(T)$, of TmAgGe above the Néel temperature has a clear Curie-Weiss behavior,¹ in contrast to the case of YbAgGe, the temperature dependence of the Hall coefficient for

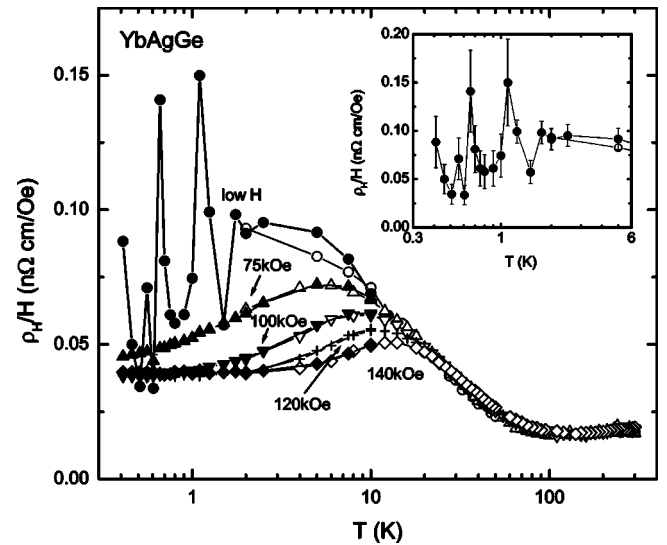


FIG. 4. Temperature-dependent Hall coefficient of YbAgGe ($H\parallel ab$) measured in different applied fields down to 0.4 K. Open symbols: He-4 measurements (2–300 K), filled symbols: measurements using He-3 option (0.4–10 K). Inset: enlarged low-temperature part of the low-field data with the estimated error bars.

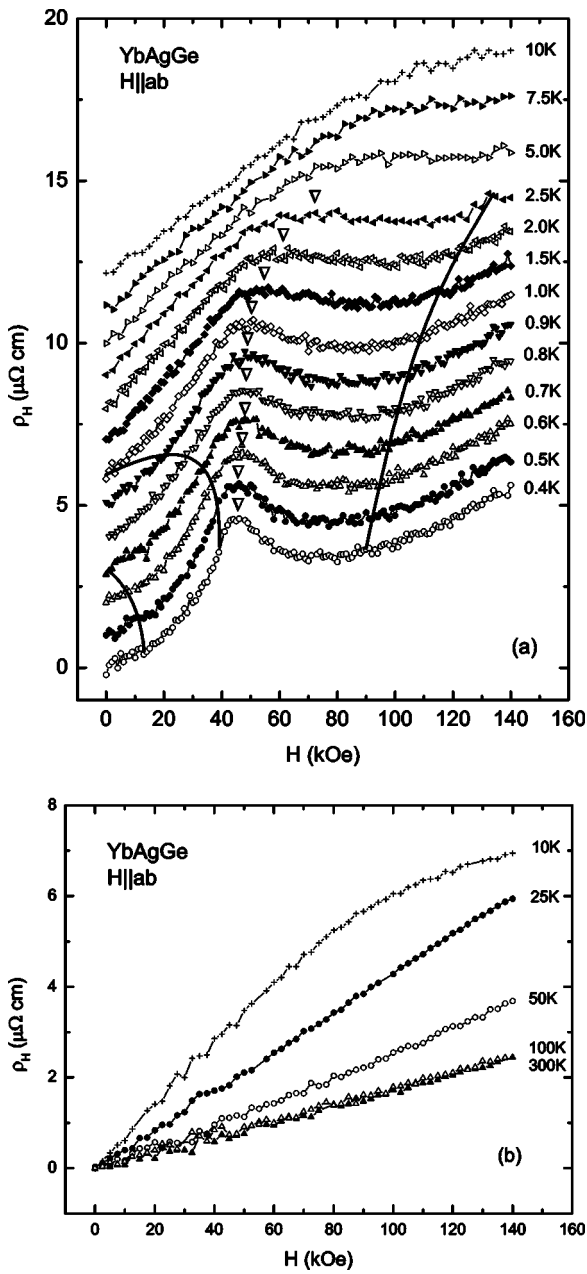


FIG. 5. Field-dependent Hall resistivity of YbAgGe ($H||ab$) measured at different temperatures: (a) low-temperature data: the curves, except for $T=0.4$ K, are shifted by $1 \mu\Omega \text{ cm}$ increments for clarity; the lines represent the phase lines from the phase diagram in Fig. 10(a) of Ref. 2; the triangles mark the position of the local maximum in $\rho_H(H)$; and (b) intermediate- and high-temperature data. Note: $T=10$ K data is shown in both plots for reference and is unshifted in (b).

TmAgGe [Fig. 1(b)] does not have a similar functional form. The reason for this difference is apparently the very small skew scattering contribution ($R_s \ll R_H^{res}$) to the Hall coefficient in TmAgGe. Similarly small couplings of local moment magnetism with the Hall effect has been seen in other rare-earth intermetallics, e.g., RNi_2B_2C (R =rare earth) borocarbides.²³⁻²⁵

In order to further explore the low-temperature behavior of the Hall coefficient, measurements down to 0.4 K were

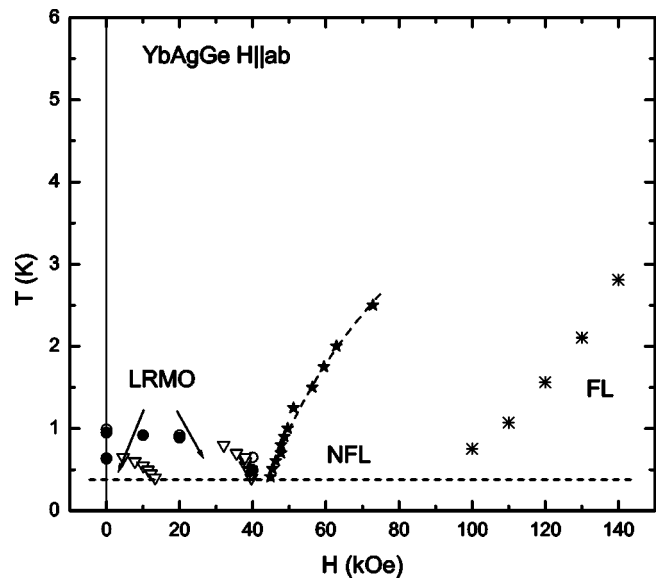


FIG. 6. Revised tentative $T-H$ phase diagram for $H||ab$. Long range magnetic-order (LRMO) and the coherence-temperature lines marked on the phase diagram are taken from Ref. 2. Filled stars and corresponding dashed line as a guide to the eye are defined from the maximum in the $\rho_H(H)$ curves.

performed. The results (on a semi-log scale) are shown in Fig. 4. The data taken in applied fields of 75 kOe and higher show the expected leveling off of the $R_H(T)$ as $T \rightarrow 0$. It is noteworthy that the measured value of $R_H(T \rightarrow 0)$ is close to the aforementioned estimate of the residual Hall coefficient. This agreement suggests that at the lowest temperatures the Hall coefficient is dominated by R_H^{res} and, barring the residual skew scattering contribution, can probe the concentration of the electronic carriers.

Whereas the higher field values of the Hall coefficient vary smoothly with temperature (Fig. 4), the low-field data, below $T \approx 3$ K, show large variations. Although the signal-to-noise ratio in the low-field measurements is inherently

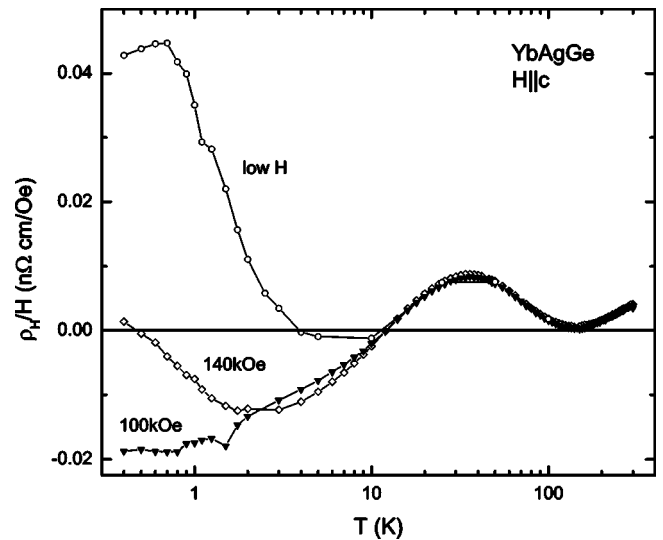


FIG. 7. Temperature-dependent Hall coefficient of YbAgGe ($H||c$) measured in different applied fields down to 0.4 K.

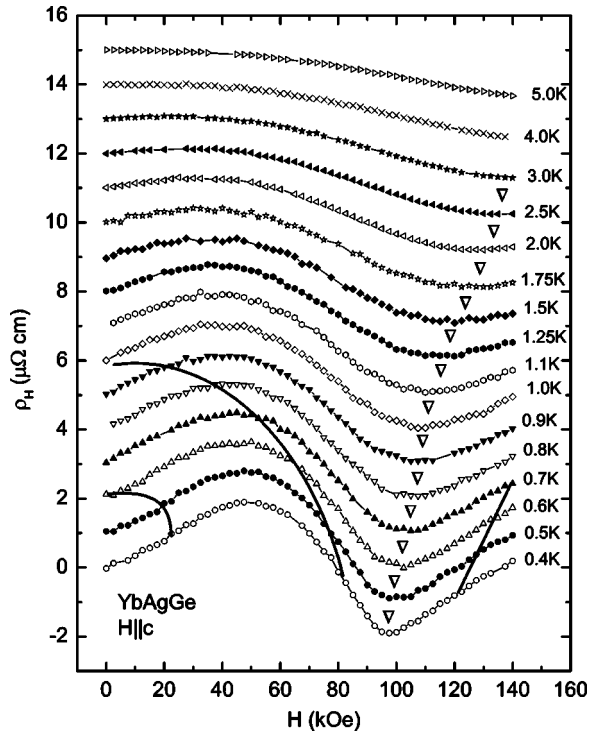


FIG. 8. Low-temperature field-dependent Hall resistivity of YbAgGe ($H\parallel c$); the curves, except for $T=0.4$ K, are shifted by $1 \mu\Omega \text{ cm}$ increments for clarity; the lines represent the phase lines from the phase diagram in Fig. 10(b) of Ref. 2; the triangles mark the position of the peak in $\rho_H(H)$.

lower, these variations appear to be above the noise level (Fig. 4, inset) and the peaks slightly above 0.6 and 1.0 K are understood as the signatures of the magnetic transitions in YbAgGe (Refs. 1, 2, and 4) that are suppressed (in this orientation) when a 75 kOe, or higher, magnetic field is applied.

To further study the field-induced QCP in YbAgGe, field-dependent Hall resistance measurements were performed at different temperatures (Fig. 5). Although the theoretical constructions are usually formulated in terms of the Hall *coefficient*, not Hall *resistivity*, in the case of YbAgGe the magnetic field itself is a control parameter for the QCP that makes the proper definition of the Hall coefficient ambiguous. We will continue presenting our data as Hall resistivity, since it is a quantity unambiguously extracted from the measurements, and leave the discussion on the suitable definition of the Hall coefficient for the Appendix.

For temperatures at and above ~ 10 K, the $\rho_H(H)$ behavior is monotonic and, at higher temperatures, eventually linear [Fig. 5(b)]. This type of behavior has been observed in a number of different materials in the paramagnetic state.¹³ The low-temperature evolution of the $\rho_H(H)$ behavior is more curious [Fig. 5(a)] and ought to be compared with the phase diagram obtained for YbAgGe ($H\parallel ab$) in Ref. 2 (an augmented version of which is shown in Fig. 6 below). The lines in Fig. 5(a) roughly connect the points according to the phase lines in Ref. 2 (see also Fig. 6 below). It can be seen that the lower H - T mag-

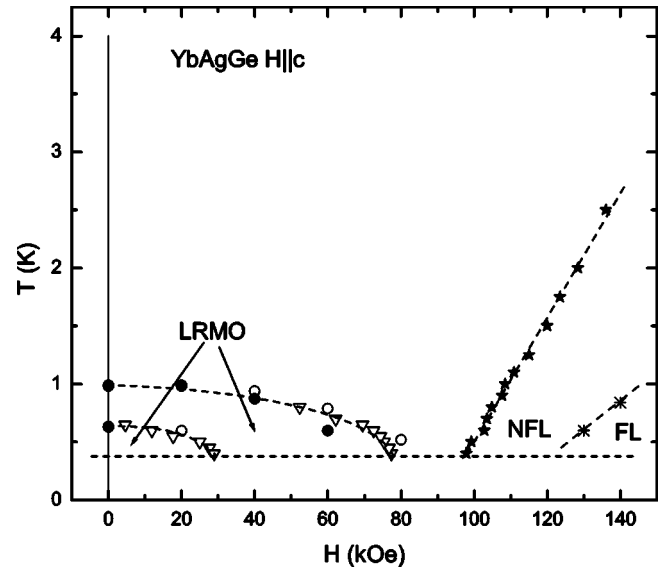


FIG. 9. Revised tentative T - H phase diagram for $H\parallel c$. Long-range magnetic order (LRMO) and the coherence temperature lines marked on the phase diagram are taken from Ref. 2. Filled stars are defined from the minimum in the $\rho_H(H)$ curves. Dashed lines are guides to the eye.

netically ordered phase line possibly has (despite the scattering of the points) correspondent features in $\rho_H(H)$, and the coherence line in Ref. 2 (and Fig. 6) roughly corresponds to the beginning of the high-field linear behavior in $\rho_H(H)$. On the other hand, the higher H - T magnetically ordered phase line cannot unambiguously be associated with any feature in $\rho_H(H)$ curves.

The most interesting feature shown in Fig. 5(a) though is the presence of the pronounced peak, or local maximum, in $\rho_H(H)$ that occurs at ≈ 45 kOe for the $T=0.4$ K curve and can be followed up to temperatures above long-range magnetic-order transition temperatures. For $T=2.5$ K a broad, local maximum in ρ_H , centered at $H\approx 100$ kOe can just barely be discerned. As temperature is reduced this feature sharpens and moves down in field. For $T=1$ K the local maximum in ρ_H is clearly located at $H\approx 50$ kOe and by $T=0.4$ K ρ_H has sharpened almost to the point of becoming discontinuous with $H_{max}\approx 45$ kOe. The temperature dependence of H_{max} is shown in Fig. 6 clearly demonstrating that as $T\rightarrow 0$, $H_{max}\rightarrow H_{crit}$ for the QCP. Independent of any theory these data clearly show that (i) ρ_H is an extremely sensitive method of determining H_{crit} of QCP, (ii) H_{max} has a clear temperature dependence, and (iii) the QCP influences ρ_H up to $T\leq 2.5$ K, a temperature significantly higher than the $H=0$ antiferromagnetic ordering temperature.

The new phase line (shown as stars in Fig. 6 associated with ρ_H maximum is distinct from the lines inferred from $C_p(T, H)$ and $\rho(T, H)$ data.² As $T\rightarrow 0$ this line approaches H_{crit} , but for finite T it is well separated from the coherence line that was determined by the onset of T^2 resistivity behavior. This new H_{max} line rather clearly locates H_{crit} at ~ 45 kOe, the field at which the long-range antiferromagnetic order appears to be suppressed.

C. YbAgGe, $H\parallel c$

Since the response of YbAgGe to an applied magnetic field is anisotropic,¹⁻⁴ it is apposite to repeat the Hall measurements for the magnetic field applied parallel to the crystallographic c axis. The temperature-dependent Hall coefficient taken in different applied fields is presented in Fig. 7 (the low-field data were obtained as described above). The $R_H(T)$ behavior for $H\parallel c$ is qualitatively similar to that for $H\parallel ab$ with a broad maximum being shifted to ~ 30 K (as compared to ~ 10 K for $H\parallel ab$) and being less sensitive to the applied field. The low-temperature, field-dependent Hall resistivity for $H\parallel c$ is shown in Fig. 8. In many aspects the overall behavior is similar to that for $H\parallel ab$: there are no apparent features associated with the phase lines derived from magnetoresistance and specific heat measurements² (shown as lines in Fig. 8), however, there is the presence of a pronounced minimum in $\rho_H(H)$ that occurs at ≈ 98 kOe for the $T=0.4$ K curve and can be followed up to the temperatures well above the zero-applied-field magnetic transition temperatures. For $T=2$ K a broad, local minimum in ρ_H , centered at $H\approx 128$ kOe can still be recognized and at $T=2.5$ K a local minima occurs just at the edge of our field range. As temperature is reduced this feature sharpens and moves down in field. The temperature dependence of H_{min} is shown in Fig. 9 clearly demonstrating that, akin to the $H\parallel ab$ case, as $T\rightarrow 0$, $H_{min}\rightarrow H_{crit}$ for the QCP. The $\rho_H(H)$ behavior for this orientation is more complex, and there is an additional, broad maximum in lower fields ($H\approx 50$ kOe at 0.4 K) that fades out with increasing temperature. This highly non-monotonic in field behavior is the origin of the dissimilarities in the low-temperature $R_H(T)$ data (Fig. 7) taken in different applied fields.

The high-field minimum in $\rho_H(H)$ (Fig. 8) defines a new phase line (shown as stars in Fig. 9) which is clearly different from the lines inferred from $C_p(T, H)$ and $\rho(T, H)$ data.² As $T\rightarrow 0$ this line approaches H_{crit} , but for finite T it is well separated from the coherence line that was determined by the onset of T^2 resistivity behavior. For this orientation of the applied field this new H_{min} line rather clearly locates H_{crit} at ~ 100 kOe, the field at which the long-range antiferromagnetic order appears to be suppressed.

It should be noted that the new lines in the $H-T$ phase diagrams were established from different types of extrema in $\rho_H(H)$, *maximum* for $H\parallel ab$ and *minimum* for $H\parallel c$. We neither consider this difference as a reason for particular discomfort nor do we necessarily view it as a potential clue to deeper understanding of the nature of the field-induced QCP in this material. The preliminary band structure calculations²² on LuAgGe, the nonmagnetic analog of the title compound, suggest that the members of the RAgGe series have a complex Fermi surface consisting of multiple sheets. In such a case a change in the Fermi surface may possibly have different signatures in the Hall measurements with different field orientation. In addition, existing QCP models appear not to be at the level of considering different shapes and topologies of the Fermi surfaces.

Whereas these new, H_{max}/H_{min} lines on the $H-T$ phase diagrams (Figs. 6 and 9) appear to be closely related with the

QCP, their detailed nature and temperature dependencies will require further experimental and theoretical attention.

IV. SUMMARY

The temperature- and field-dependent Hall resistivity have been measured for YbAgGe single crystals with $H\parallel ab$ and $H\parallel c$ orientation of the applied magnetic field. The temperature-dependent Hall coefficient of YbAgGe behaves similarly to other heavy fermion materials. Low-temperature, field-dependent measurements reveal a local maximum ($H\parallel ab$) or minimum ($H\parallel c$) in $\rho_H(H)$ for $T\leq 2.5$ K that occurs at a value that approaches $H_{crit}\approx 45$ kOe ($H\parallel ab$) and $H_{crit}\approx 90$ kOe ($H\parallel c$) as $T\rightarrow 0$. These data indicate that (i) the Hall resistivity is indeed a useful measurement for the study of QCP physics and (ii) the influence of the QCP extends to temperatures significantly higher than the $H=0$ antiferromagnetic ordering temperature.

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APPENDIX

Coleman *et al.*⁹ suggest that $R_H(P)$ data (where P is a control parameter, i.e., H in our case) can be used to distinguish between two possible QCP scenarios: diffraction off of a critical spin density wave or a breakdown of the composite nature of the heavy electron, with the former manifesting a change of slope at P_{crit} and the latter manifesting a divergence in the slope of $R_H(P)$ at P_{crit} . Since in our case the magnetic field is itself the control parameter, it is not clear if $R_H=\rho_H/H$, $R_H=d\rho_H/dH$, or just simply ρ_H should be used for comparison with the theory. $R_H(H)$ curves determined by two aforementioned ways are presented in Figs. 10 ($H\parallel ab$) and 11 ($H\parallel c$). For both definitions and both orientations the evolution of a clear feature in $R_H(H)$ (defined as a local extremum for ρ_H/H and as a midpoint between two different field-dependent regimes for $d\rho_H/dH$) replicates (albeit with slight H -shift) the behavior of the Hall resistivity [Figs. 5(a) and 8]. Given that the new phase line in Figs. 6 and 9 is fairly insensitive to the data analysis we feel that the use of $\rho_H(H)$ data is currently the least ambiguous data set to analyze. On the other hand, if the form of the anomaly near H_{crit} is to be analyzed in detail it will be vital to have a more detailed theoretical treatment of magnetotransport in field-induced QCP materials.

It is tempting to say that for the case of applied field as a control parameter the quantity $d\rho_H(H)/dH$ [rather than $\rho_H(H)/H$] serves the role of the low-field Hall coefficient and should be compared with the prediction of the models. If this point of view is accepted, then for $H\parallel ab$ the shape and evolution of the $d\rho_H(H)/dH$ curves [Fig. 10(b)] suggest that

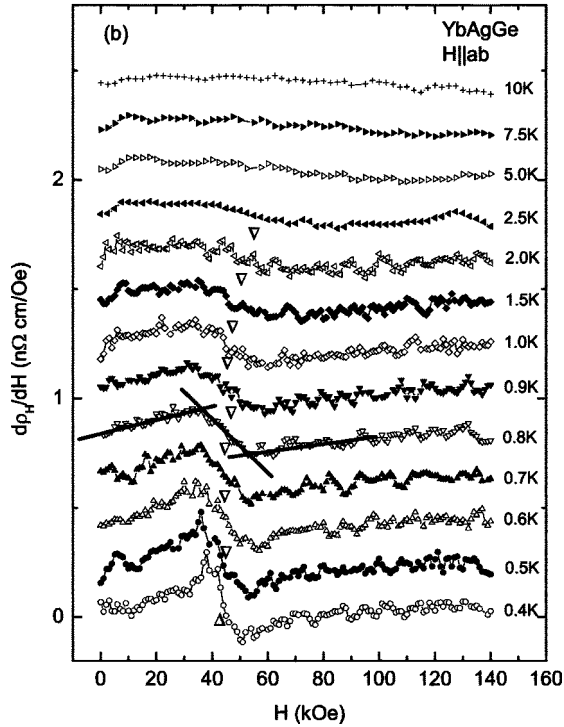
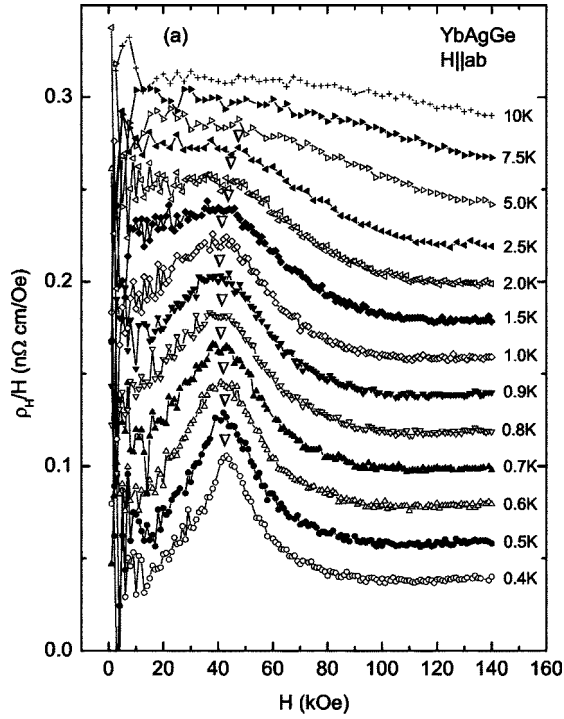


FIG. 10. Field-dependent Hall coefficient of YbAgGe ($H\parallel ab$), defined as (a) $R_H = \rho_H/H$ and (b) $R_H = d\rho_H/dH$, measured at different temperatures. The curves, except for $T = 0.4$ K, are shifted by (a) 0.02 nΩ cm and (b) 0.2 nΩ cm increments for clarity; the triangles mark the position of the feature in $R_H(H)$: a local maximum in ρ_H/H and a midpoint of the transition between two different field-dependent regimes (see, e.g., 0.8 K curve) in $d\rho_H/dH$. Curves in the (b) panel were obtained by differentiation of the five-adjacent-points-smoothed $\rho_H(H)$ data. The small downturn at $H \geq 130$ kOe in some $d\rho_H/dH$ curves [panel (b)] is most likely an artifact of using digital smoothing and differentiation.

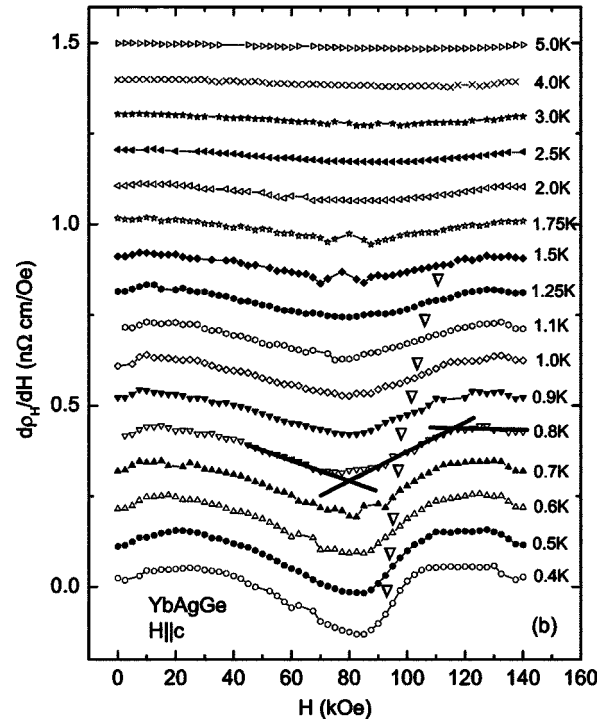
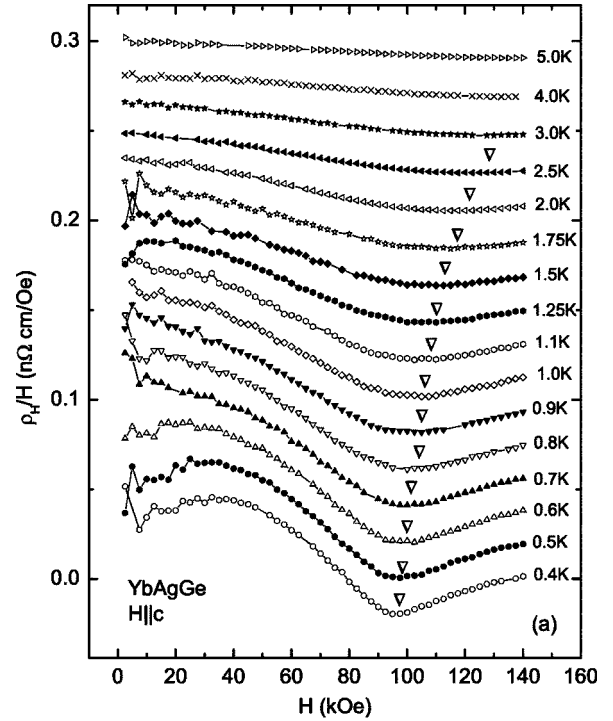


FIG. 11. Field-dependent Hall coefficient of YbAgGe ($H\parallel c$), defined as (a) $R_H = \rho_H/H$ and (b) $R_H = d\rho_H/dH$, measured at different temperatures. The curves, except for $T = 0.4$ K, are shifted by (a) 0.02 nΩ cm and (b) 0.1 nΩ cm increments for clarity; the triangles mark the position of the feature in $R_H(H)$: a local minimum in ρ_H/H and a midpoint of the transition between two different field-dependent regimes (see, e.g., 0.8 K curve) in $d\rho_H/dH$. Curves in the (b) panel were obtained by differentiation of the five-adjacent-points-smoothed $\rho_H(H)$ data. The small downturn at $H \geq 130$ kOe in some $d\rho_H/dH$ curves [panel (b)] is most likely an artifact of using digital smoothing and differentiation.

possibly the composite fermion model of the QCP is more relevant to the case of YbAgGe, although for $H\parallel c$ the shape and evolution of the $d\rho_H(H)/dH$ curves [Fig. 11(b)] are at variance with the simple theoretical views. The lack of the

$T < 0.4$ K data and an absence of a more detailed, realistic-Fermi-surface-tailored, model do not allow us to choose the physical picture of the field-induced QCP in YbAgGe unambiguously.

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